

'समानो मन्त्रः समितिः समानी'

UNIVERSITY OF NORTH BENGAL

B.Sc. Honours 2nd Semester Examination, 2022

GE1-P2-STATISTICS

FUNDAMENTAL OF PROBABILITY THEORY

Time Allotted: 2 Hours Full Marks: 40

The figures in the margin indicate full marks. All symbols are of usual significance.

GROUP-A

1. Answer any *five* questions:

 $1 \times 5 = 5$

- (a) If $P(A \cup B) = \frac{5}{6}$, $P(A \cap B) = \frac{1}{3}$ and $P(A^c) = \frac{1}{2}$, then show that A and B are independent.
- (b) The mean and variance of a binomial variate X are 4 and $\frac{4}{3}$. Find P(X = 1).
- (c) Show that the chance of throwing an odd number with a die is $\frac{1}{2}$.
- (d) What is the chance that a non-leap year selected at random will contain 53 Sundays?
- (e) For a binomial distribution with mean 5 and S.D. 2, find the mode.
- (f) For what value of k, $f(x, y) = ke^{-(x+y)}$, $x \ge 0$, $y \ge 0$ will represent probability density function?
- (g) State the Central Limit Theorem.
- (h) State two properties of hypergeometric distribution.

GROUP-B

2. Answer any *three* questions:

 $5 \times 3 = 15$

- (a) State and prove Bayes' Theorem.
- (b) Prove that the variance of binomial distribution is *npq*.
- (c) Derive Poisson distribution as the limit of binomial distribution.
- (d) Two persons toss a true coin n times each. Show that the probability of their scoring the same number of heads is $\binom{2n}{n} 2^{-2n}$.

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(e) If X follows binomial distribution with parameter n and p then prove that

$$P[X \text{ is even}] = \frac{1}{2}[1 + (q - p)^n] \text{ where } p + q = 1$$

GROUP-C

3. Answer any *two* questions:

 $10 \times 2 = 20$

- (a) (i) Show that the expectation of the product of two independent random variables is equal to the product of their expectations.
 - (ii) Show that for the binomial distribution

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$$\mu_{r+1} = p(1-p)\left(nr\mu_{r-1} + \frac{d\mu_r}{dp}\right)$$

where the symbols have their usual meanings.

- (b) (i) In a distribution exactly normal, 7% of the items are under 35 and 89% are under 63, what are the mean and s.d. of the distribution?
 - (ii) Find the points of inflextion of the normal curve. 5
- (c) (i) For a normal distribution show that odd order moments about mean are zero.
 - (ii) Find the probability that at most 5 defective fuses will be found in a box of 200 fuses, if experience show that 2% of such fuses are defective.
- (d) (i) Find the mode of the Poisson distribution.
 - (ii) A coin is tossed until a head appears. What is the expectation of the number of tosses?



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