



'সমানো মন্ত্র: সমিতি: সমানী'

## UNIVERSITY OF NORTH BENGAL

B.Sc. Honours 5th Semester Examination, 2021

### DSE-P2-PHYSICS

*The figures in the margin indicate full marks.  
All symbols are of usual significance.*

**Candidates should also ensure that the chosen section in the paper DSE-2 is different from the chosen section in the paper DSE-1.**

**The question paper contains paper DSE-2A, DSE-2B and DSE-2C.  
The candidates are required to answer any *one* from *three* sections.  
Candidates should mention it clearly on the Answer Book.**

### DSE-2A

#### NANO-MATERIALS AND APPLICATIONS

**Time Allotted: 2 Hours**

**Full Marks: 40**

#### GROUP-A

1. Answer any *five* questions from the following: 1×5 = 5
- (a) Which factor causes the properties of nano-materials to differ significantly from other materials? 1
  - (b) Which nano-materials is used for cutting tools? 1
  - (c) A carbon monoxide sensor made of zinconia uses which characteristic to detect any charge? 1
  - (d) If the atomic numbers of zirconium, molybdenum, palladium and tin are 40, 42, 46 and 50 respectively, which will be suitable filter for X-radiation from molybdenum? 1
  - (e) Define Band gap. 1
  - (f) What do you mean by nanowires? 1
  - (g) Define grain boundary of a nanoparticle. 1
  - (h) What is a quantum-dot laser? 1

#### GROUP-B

**Answer any *three* questions from the following** 5×3 = 15

2. (a) Define Bragg's law. 2
- (b) Find the longest wavelength that can be used to analyse a NaCl crystal of interplanar spacing 0.281 nm between its principal planes in first order. 3

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|--|---|
| 3. (a) Distinguish between direct and indirect band gap.                           | 3 |
| (b) What is exciton? Explain.  | 2 |
| 4. Discuss in detail application of nanosensor systems.                            | 5 |
| 5. Explain in detail why band gap of nano-materials increases with size reduction. | 5 |
| 6. Discuss in detail different types of ball-milling and their advantages.         | 5 |

**GROUP-C**

Answer any *two* questions from the following

10×2 = 20

- |   |     |
|---|-----|
| 7. Discuss several bottom up approaches to synthesize nano-materials.   | 10  |
| 8. List out applications of nano-materials and neatly explain them.   | 10  |
| 9. (a) Explain exciton generation and its transport in quantum dots.  | 6   |
| (b) What is the difference between SEM and STM?   | 4   |
| 10.(a) Explain Coulomb interactions in a dielectric quantum nanostructure.  | 4   |
| (b) Calculate the self energy and charging energy when the quantum dot is embedded in a semi-conductor with large band gap. | 3+3 |

**DSE-2B**

**ADVANCED MATHEMATICAL PHYSICS-I**

**Time Allotted: 2 Hours**

**Full Marks: 40**

**GROUP-A**

- |  |         |
|--|---------|
| 1. Answer any <i>five</i> questions from the following:  | 1×5 = 5 |
| (a) Find the Laplace transform of the signal   | 1       |
| $x(t) = te^{-2 t }$ .  |         |
| (b) Draw the graph of $\theta(t-a) - \theta(t-b)$ . $\theta$ is defined as step functions $a$ and $b$ are arbitrary constant.            | 1       |
| (c) Show that $\vec{a} = 2\hat{i} + 3\hat{j} + 5\hat{k}$ and $\vec{b} = 6\hat{i} + 9\hat{j} + 15\hat{k}$ do not form any closed surface. | 1       |
| (d) If $A$ is a $(n \times n)$ antisymmetric matrix, show that $ A  = 0$ when $n$ is an odd integer number.                              | 1       |

- (e) Find the dimension of the subspace of  $M_{2 \times 2}$  spanned by, 1
- $$\begin{pmatrix} 1 & -5 \\ -4 & 2 \end{pmatrix}, \begin{pmatrix} 1 & 1 \\ -1 & 5 \end{pmatrix}, \text{ and } \begin{pmatrix} 2 & -4 \\ -5 & -7 \end{pmatrix}$$
- (f) Two directions  $\vec{n}$  and  $\vec{n}'$  are defined in a spherical coordinate system by the angles  $\theta, \alpha$  and  $\theta', \alpha$  respectively. Find the cosine of the angle between them. 1
- (g) Write down the basis of a rank-2 tensor in 2-dimension. 1
- (h) Calculate  $\delta_{ii}$  in 3-dimension. 1

**GROUP-B**

**Answer any three questions from the following**

5×3 = 15

2. Obtain Inverse Laplace Transform of 5

$$\frac{s}{1 + s^2 + s^4}$$

3. (a) Define a linear functional on a vector space. 2
- (b) Consider the vector space  $\mathbb{R}[x]$  of all polynomials over the field  $\mathbb{R}$  of real numbers. Show that the mapping  $f(x) \rightarrow \int_0^1 f(x) dx; f(x) \in \mathbb{R}[x]$  is a linear functional on  $\mathbb{R}[x]$ . 3
4. (a) Write down the condition on which a subset of a vector space can be called linearly dependent. 2
- (b) Check the linear independency of the set, 3
- $$S = \{(1, 3, -4, 2), (2, 2, -4, 0), (1, -3, 2, -4), (-1, 0, 1, 0)\} \text{ in } \mathbb{R}^4.$$
5. (a) Construct a scalar from the tensor  $A_{kl}^{ij}$ . 3
- (b) Define metric tensor. 2
6. (a) Find out the basis transformation matrix ( $S$ ) in 3-D when the Cartesian coordinate is rotated with an angle  $\theta$  about  $x$ -axis. 2
- (b) The vector field  $\vec{a}$  satisfies  $\nabla \cdot \vec{a} = 0$  inside some volume  $V$  and  $\vec{a} \cdot \hat{n} = 0$  on the boundary surface  $S$ .  $\hat{n}$  is the unit vector along  $\vec{S}$ . By considering the divergence theorem applied to  $T_{ij} = x_i a_j$ , show that  $\int_V \vec{a} dV = 0$ . 3

**GROUP-C**

**Answer any two questions from the following**

10×2 = 20

7. Solve the initial value problem 10

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + 5y = 0,$$

Where,  $y = 2$  at  $x = 0$ ,  $\frac{dy}{dx} = -4$  at  $x = 0$ .

8. (a) What do you mean by the linear ‘dimension’ of a vector space? 2  
 (b) Justify whether every subspace of a finite dimensional vector space is finite dimensional or not. 3  
 (c) Find the dimension of the vector space formed by all  $(2 \times 2)$  matrices. 3  
 (d) Explain with examples whether the dimension of a vector space depends on its field or not. 2

9. Let,  $A = \begin{bmatrix} 1 & 2 & 1 & 0 & 0 \\ 1 & 2 & 2 & 2 & 3 \\ -1 & -2 & 0 & 2 & 3 \end{bmatrix}$ .

- (a) Solve  $Ax = 0$  and characterize the null space through its basis. 3  
 (b) What is the rank of  $A$ ? What are the dimensions of the column space, row space and left null space of  $A$ ? 2

- (c) Find the complete solution of  $Ax = b$ , where  $b = \begin{pmatrix} 1 \\ 2 \\ 0 \end{pmatrix}$ . 3

- (d) Find the conditions on  $b_1, b_2, b_3$  that ensure  $Ax = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$  has a solution. 2

- 10.(a) Show that, in general coordinates, the quantities  $\frac{\partial v^i}{\partial u^j}$  do not form the components of a tensor. 3  
 (b) Prove that  $\delta_j^i$  is a mixed second rank tensor. 2  
 (c) A covariant rank-1 tensor has components  $xy, 2y - z^2, xz$  in rectangular coordinates. Find its covariant components in spherical coordinates. 5

**DSE-2C**  
**CLASSICAL DYNAMICS**

Time Allotted: 2 Hours

Full Marks: 60

**GROUP-A**

1. Answer any *four* questions from the following: 3×4 = 12
- (a) Prove that a possible Lagrangian for a free particle is, 3
- $$L = \dot{q}^2 - q\dot{q}$$
- (b) What are the Lagrange's equations for a non-conservative system? 3
- (c) What do you mean by stable and unstable equilibrium? Give examples. 3
- (d) Discuss the importance of invariant interval in special theory of relativity. 3
- (e) What are space-like, time-like intervals and light-like intervals? 3
- (f) What is the meaning of critical velocity and turbulent motion? 3

**GROUP-B**Answer any *four* questions from the following

6×4 = 24

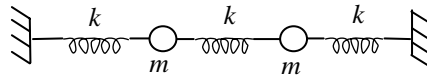
2. The Lagrangian of an anharmonic oscillator is,  $L(x, \dot{x}) = \frac{1}{2}\dot{x}^2 - \frac{1}{2}\omega^2 x^2 - dx^3 + \beta x\dot{x}^2$ . 6
3. Show that the motion of a particle under central force is planar. 6
4. A particle moving under a central force describes a spiral orbit given by  $r = ae^{b\theta}$ , where  $a, b$  are constants. Obtain the force law. 6
5. (a) What do you mean by light cone? Explain in 3-dimensional space. 3
- (b) Explain longitudinal Doppler effect using 4-vector perspective. 3
6. Obtain the normal coordinates of a system of which the Lagrangian is given by 6
- $$L = \frac{1}{2}(m_1\dot{x}^2 + m_2\dot{y}^2) + \beta\dot{x}\dot{y} - \frac{1}{2}(x^2 + y^2). \quad m_1, m_2 \text{ and } \beta \text{ being constants.}$$
7. Obtain the equation of continuity for a fluid flow. 6

**GROUP-C**Answer any *two* questions from the following

12×2 = 24

8. (a) Explain the meaning of conjugation space. 2
- (b) Show that symmetry in the Lagrangian leads to different constants of motion. 10

9. Two masses, each equal to  $m$  are connected by massless springs of spring constant  $k$ , such that they can freely slide on a smooth horizontal surface. The ends of the spring are fixed to vertical walls.



Determine:

- |                               |   |
|-------------------------------|---|
| (a) the normal frequencies.   | 4 |
| (b) normal modes of vibration | 4 |
| (c) the normal coordinates.   | 4 |
- 10.(a) What do you mean by Minkowski space and define what are world lines? 4
- (b) Explain the geometric interpretation of length contraction and time dilation using space time diagrams. 8
- 11.(a) A central attractive force varies as  $r^m$ . The velocity of a particle in a circular orbit of radius  $r$  is twice the escape velocity from the same radius. Find  $m$ . 4
- (b) Show that ordinary 3-vector momentum is not conserved under Lorentz transformation whereas the 4-vector momentum is conserved under the Lorentz transformation. 8

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